



KENTUCKY CENTER  
FOR MATHEMATICS

# Constructing Number Sense

## Fluency with Multi-digit Multiplication and Division

# Welcome!

Your host:

**Belle Rush**



Regional Consultant  
Kentucky Center for Mathematics  
[bsrush180@yahoo.com](mailto:bsrush180@yahoo.com)

# Kentucky Center for Mathematics

- KCM seeks to advance the knowledge and practice of effective mathematics teaching and learning, encompassing early childhood through adult education.
- KCM provides and develops statewide leadership, facilitate professional learning experiences, and cultivate innovation with the aim of improving mathematics education, practice and policy.

## KCM Yearly Numbers

29 math courses taught

73 cohorts of teachers

Over 1000 KY teachers  
attending

Over 182 days of  
math professional learning

Over \$150,000 of math  
materials directly in the hands  
of teachers

109 school districts

300 KY schools

100 principals trained

>5000 students impacted

KCM Annual Math Conference  
national prominence

Closing the achievement gap  
for our KY math students.

Math Achievement Fund  
intervention students (3000)  
had an average of 10 percentile  
points gained as a direct result  
of KCM trained math  
interventionists.

# Visit Our Website

[www.kentuckymathematics.org](http://www.kentuckymathematics.org)



HOME

MAF

PROFESSIONAL  
LEARNING▼

RESOURCES▼

ANNUAL  
CONFERENCE▼

ABOUT US▼



Find resources to help you engage learners, allowing them to make sense of mathematics and develop problem solving skills.

# Agenda

- What the research and standards say
- A quick look at strategies
  - Arrays and area models
  - Partial products
  - Properties of operations, especially the distributive property
- Games
  - Build It, Draw It, Prove It
  - Multi-Digit Multiplication Math Story Matching
  - Nice and Easy
- Links to manipulatives, games, and explanations of strategies

# What the research says.....

Multiplication moves from the first year (in Grade 4) where the approach of the standard algorithm is developed and explained using **visual models (diagrams)** to the second year (in Grade 5) where the approach of the standard algorithm continues to be deepened and then is used fluently.

The major issue for multi-digit multiplication is what to multiply by what and how the place values of the digits in the factors affect the place values of the partial products. An **array or area model** can help students understand these issues in terms of how the **partial products** are recorded.

NCSM JOURNAL • FALL/WINTER 2012-2013

# Critical areas for 4th grade

In the Number and Operations in Base Ten domain, students will:

apply their understanding of models for multiplication (equal-sized groups, **arrays, area models**), **place value and properties of operations**, in particular the **distributive property**, as they develop, discuss and use efficient, accurate and generalizable methods to compute products of multi-digit whole numbers;

# What do the standards say?

## KY.4.NBT.5 Multiply whole numbers

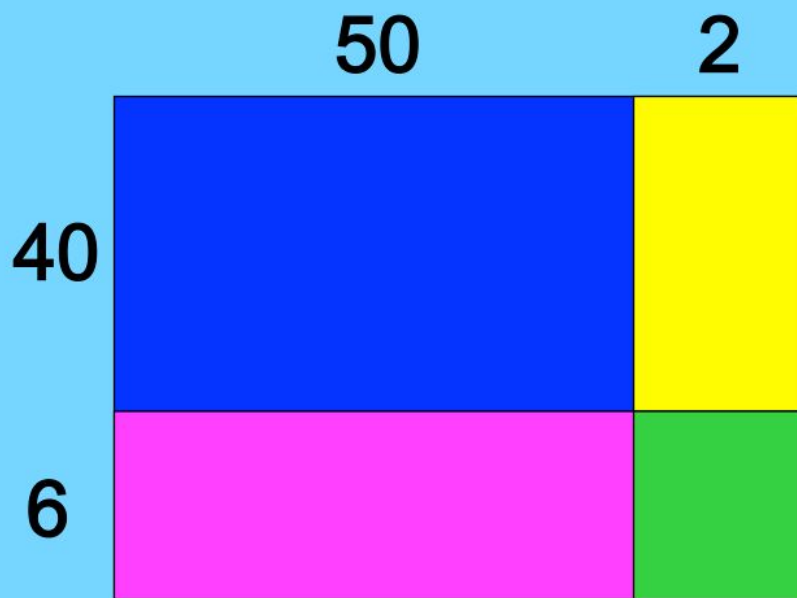
- Up to four digit number by a one-digit number
- Two-digit number by two-digit number

Multiply using strategies based on place value and the **properties of operations**. Illustrate and explain the calculation by using equations, **rectangular arrays and/or area models**. MP.3, MP.4, MP.8



# Example of area model

A Geometrical Representation  
of Partial Products  
(Area Model)



$$\begin{array}{r} 52 \\ \times 46 \\ \hline \end{array}$$

---

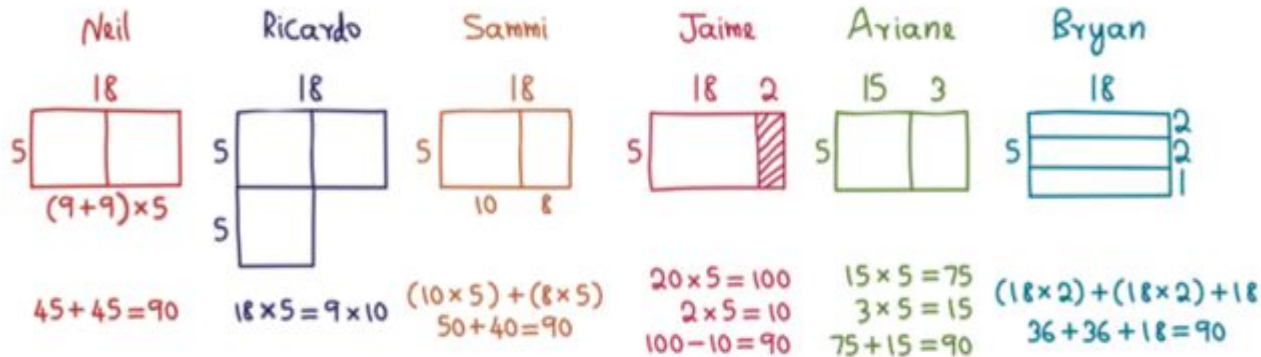
# Multiplication strategies

Partial Products	Area Model
$\begin{array}{r} 324 \\ \times 6 \\ \hline 24 \\ 120 \\ 1,800 \\ \hline 1,944 \end{array}$	$\begin{array}{r} \times \quad 300 \quad 20 \quad 4 \\ 6 \quad \boxed{1,800} \quad \boxed{120} \quad \boxed{24} \\ 1,800 + 120 + 24 = 1,944 \end{array}$

# Useful explanations of strategies

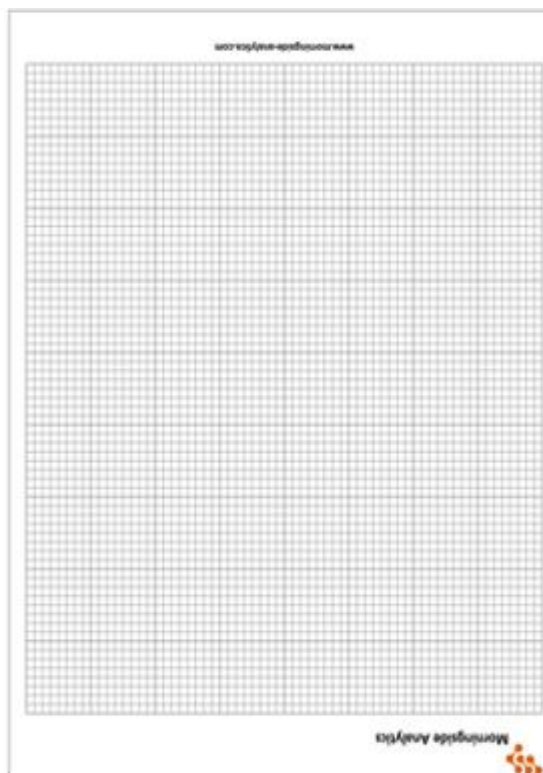
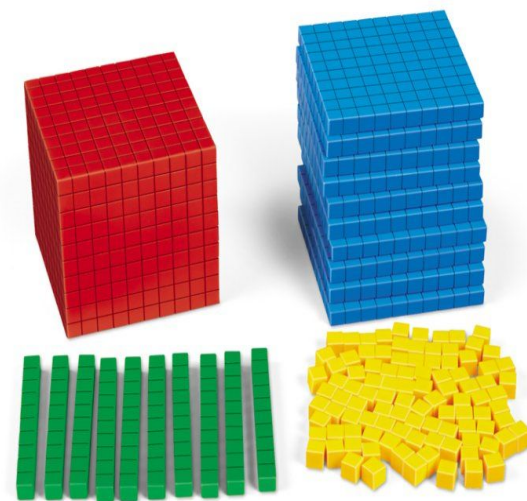
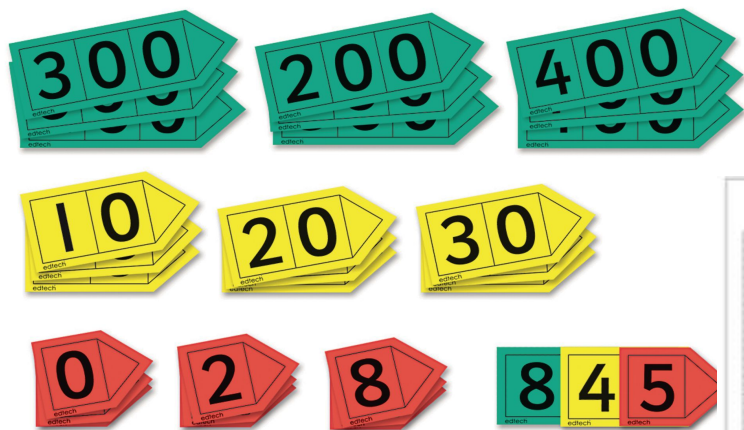
<https://www.youtube.com/watch?v=wxE2Kur4AHc>

Work out  $18 \times 5$  and show a visual solution.

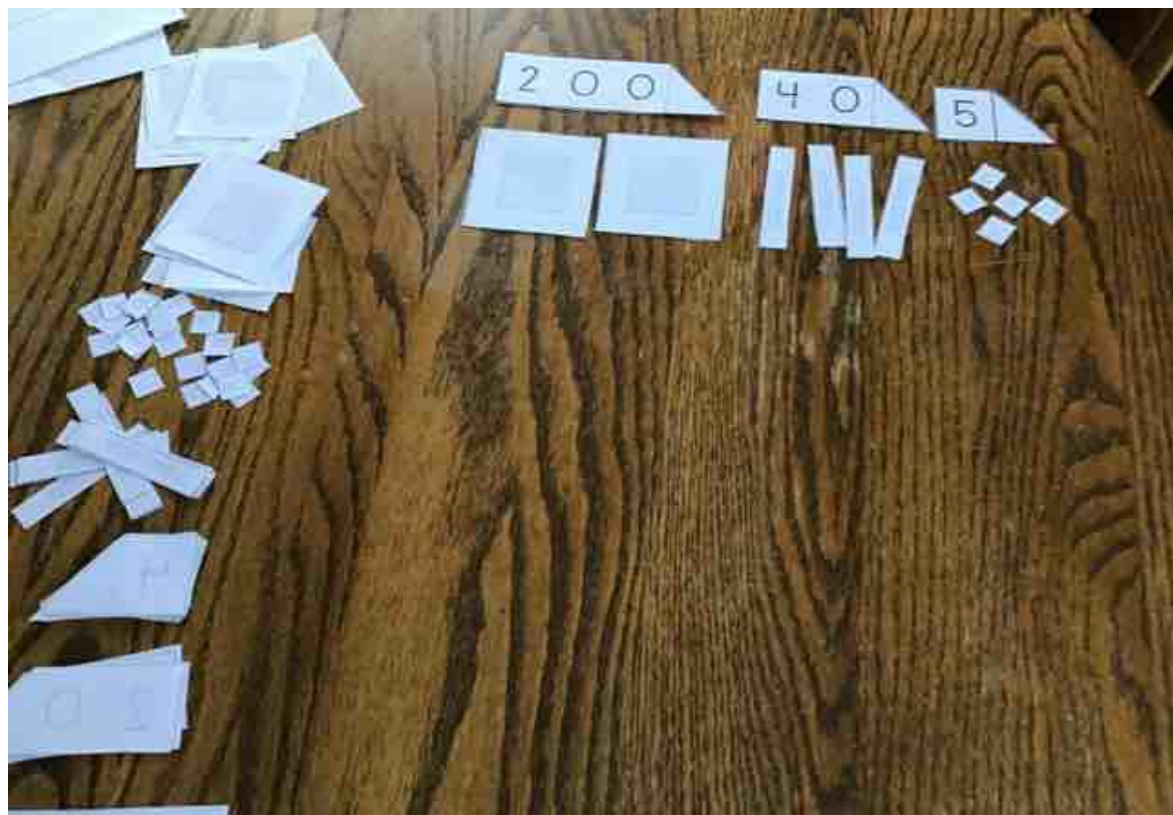


from Jo Boaler. Mathematical Mindsets (2016)

# Build It, Draw It, Prove It

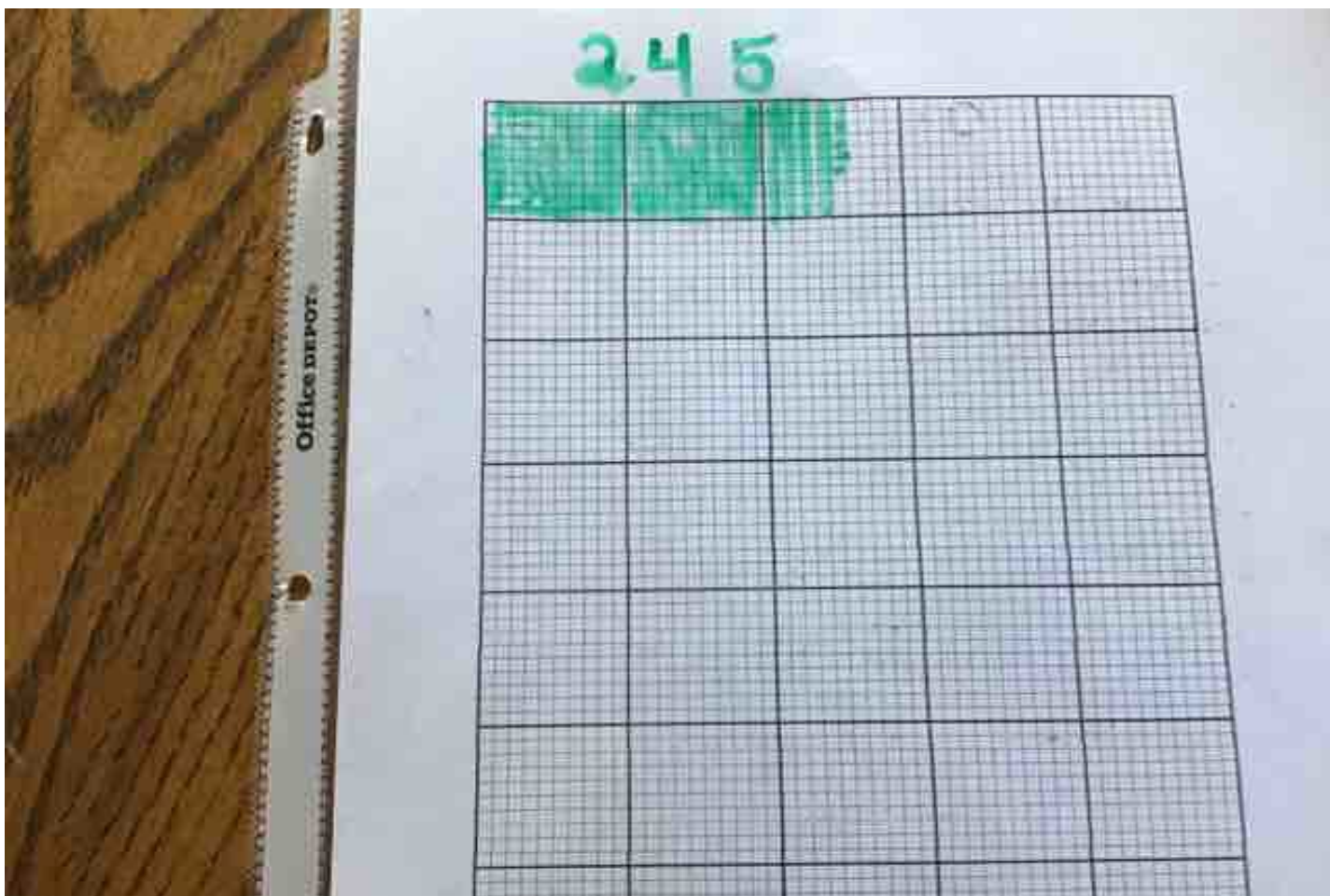


- Turn arrow cards face down.
- Turn over one from each set to create a
- 3 digit number.
- Build that number using place value pieces.

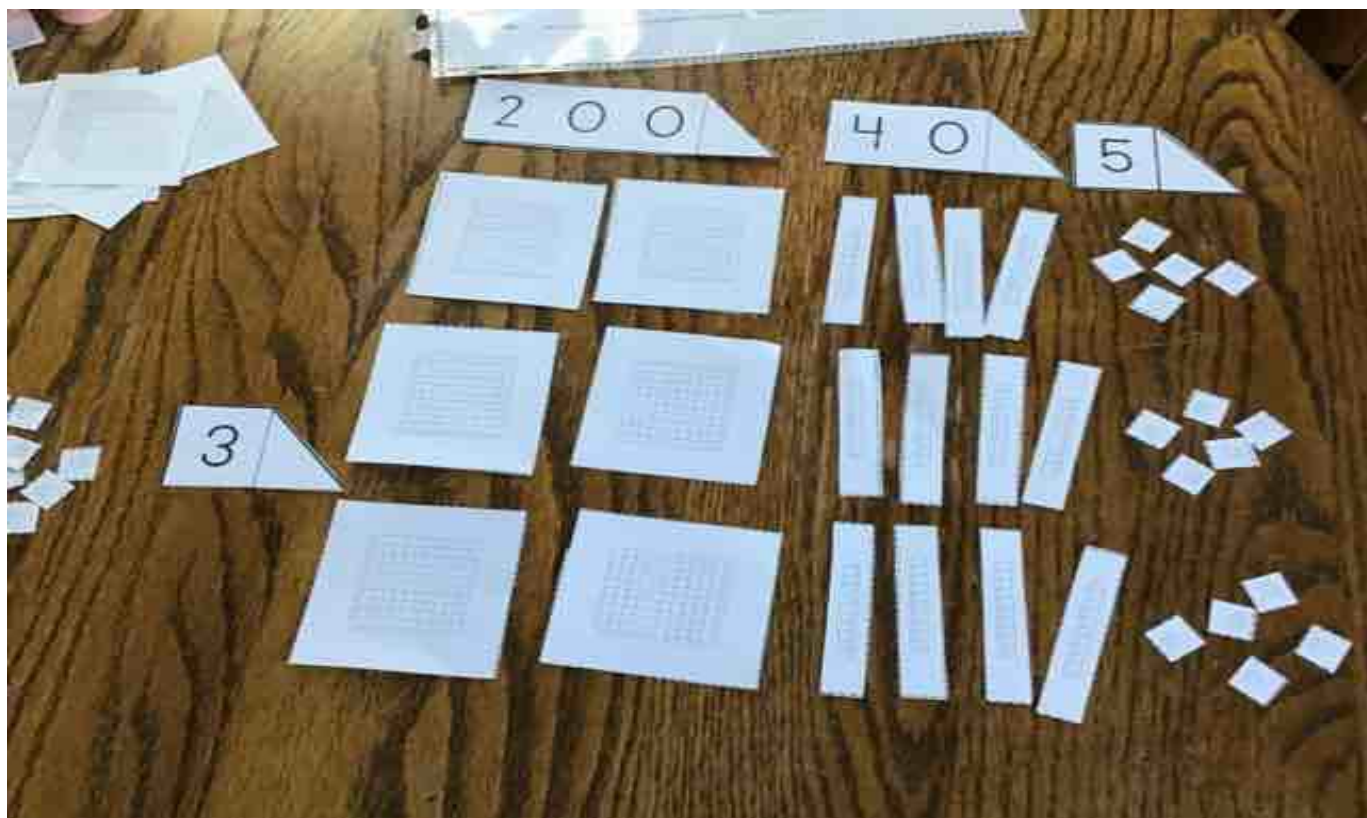




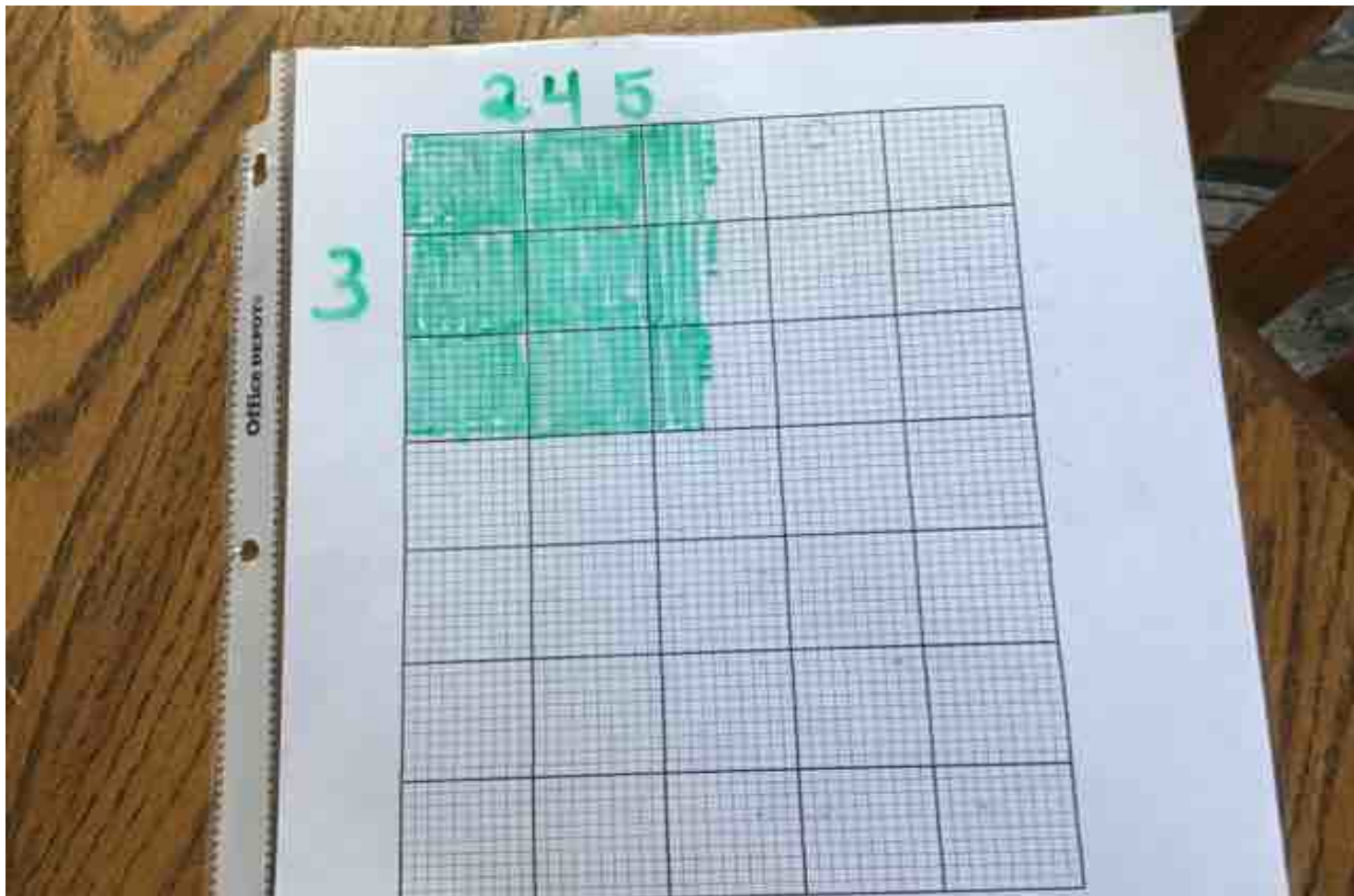
- Draw your 3 digit number on the grid paper.



- Pick up a one digit arrow card.
- Build your original number that many times with place value pieces.

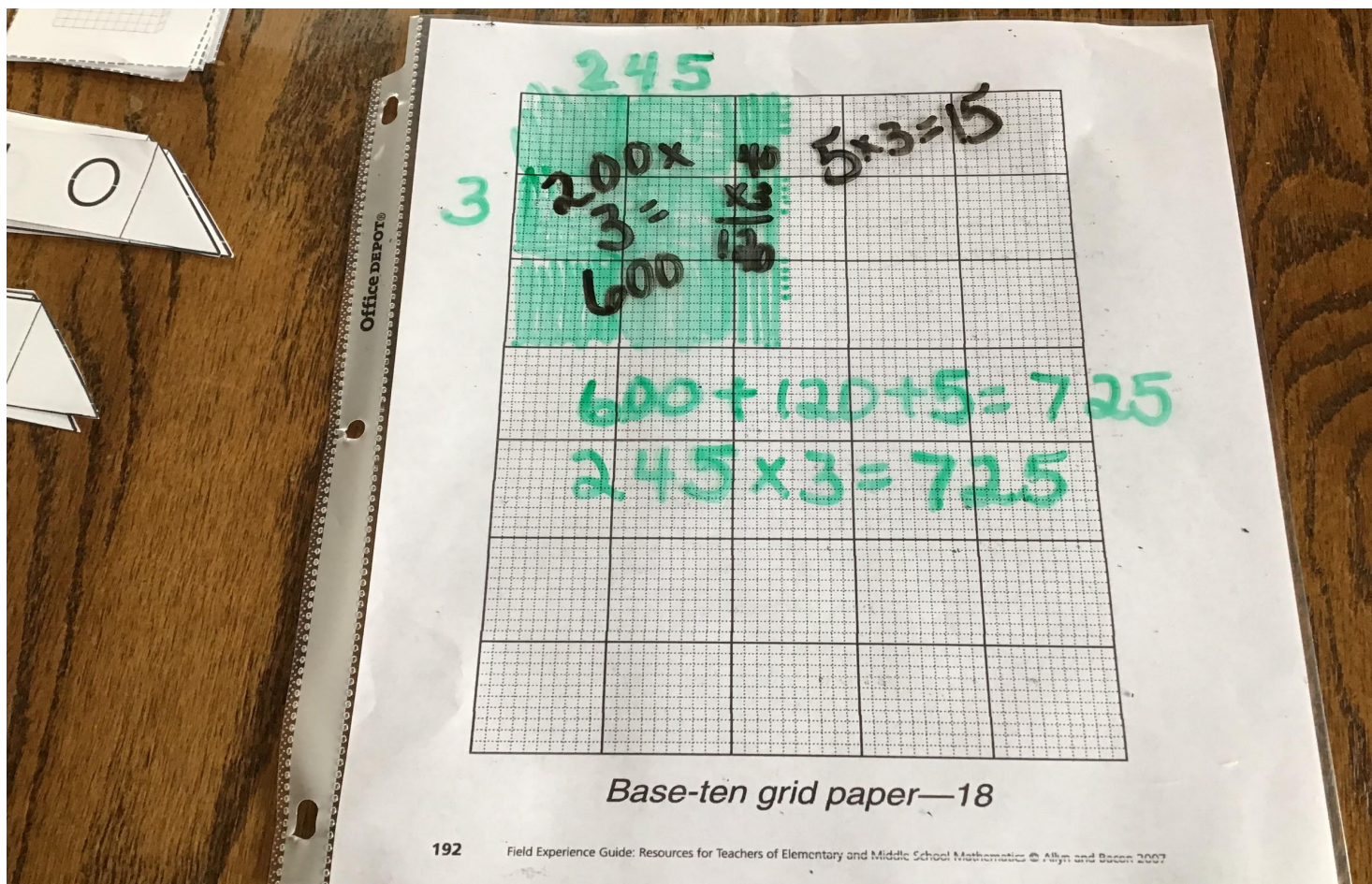


- Fill in the grid sheet, showing the total number.





- Write your equation to show how you got your answer.



# Build it, Draw it, Prove it

To play Build it, Draw it, Prove it:

1. Partner A draws an arrow cards from the hundreds, tens and ones pile
2. Partner A builds the three digit number using the base ten blocks
3. Partner A draws the model of the three digit number on the grid paper.
4. Partner A draws another arrow card this time from only the ones pile. This card is your multiplier. Partner A now has a 3 digit number times a one digit number.
5. Partner A draws the multiplication equation on the grid paper. (245 x 3) This shows the visual model of this multiplication equation.
6. Partner A solves the equation.

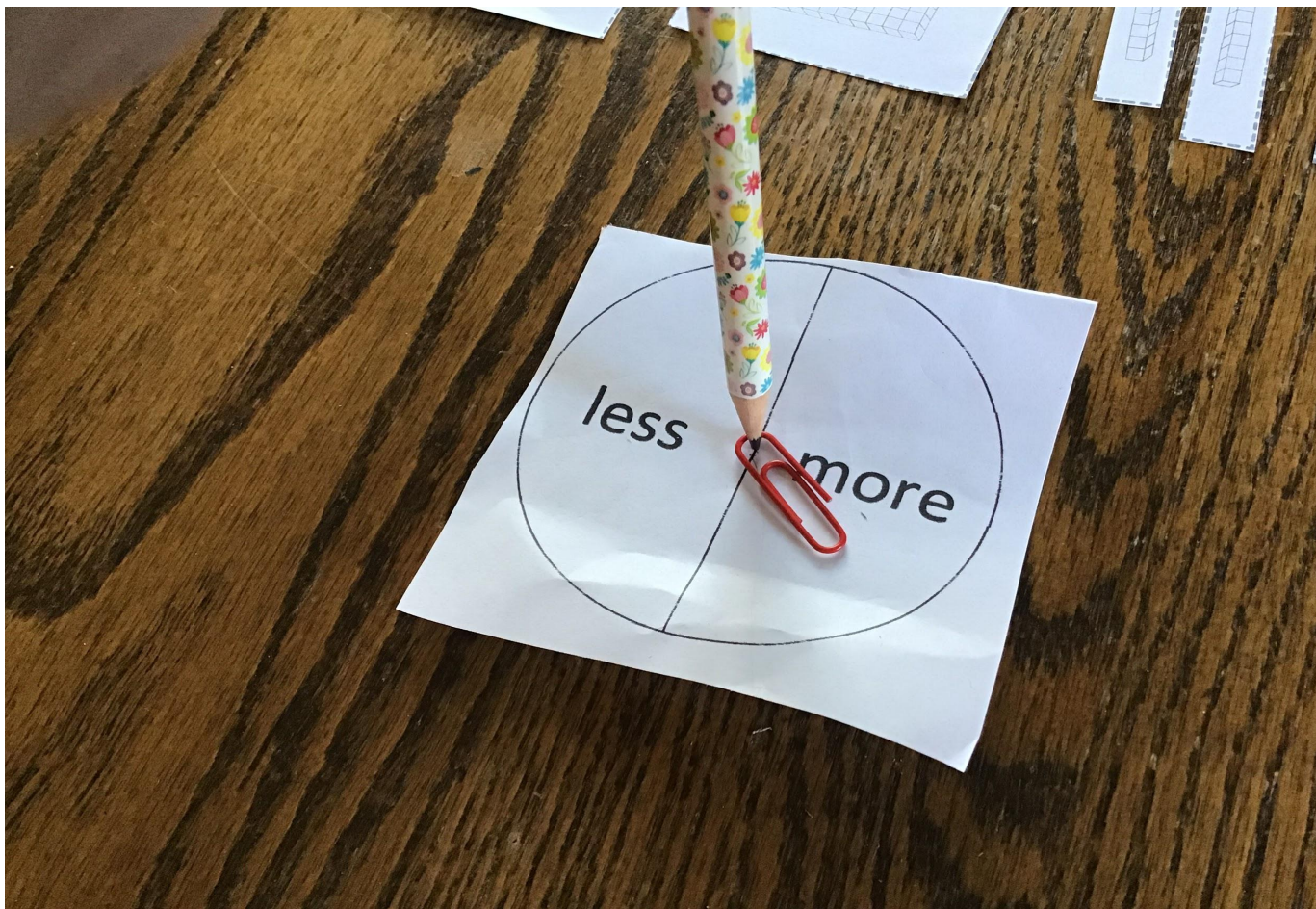
# To play it with a partner

Game:

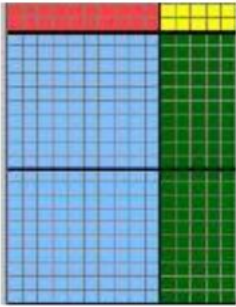
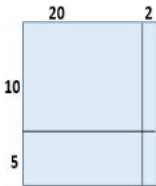
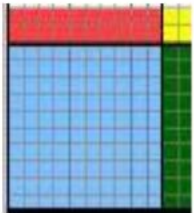
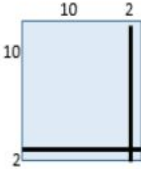
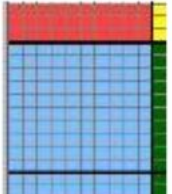
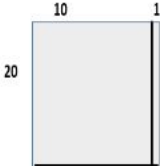
1. Partner B repeats steps 1-6
2. One partner spins the more or less spinner.
3. Winner is the partner who is either more or less based on the spinner.
4. The winning partner gets a point
5. The winner is the partner who gets 5 points first.



- If playing with a partner, after each player has had a turn, spin to see if the player with more or less gets a point.



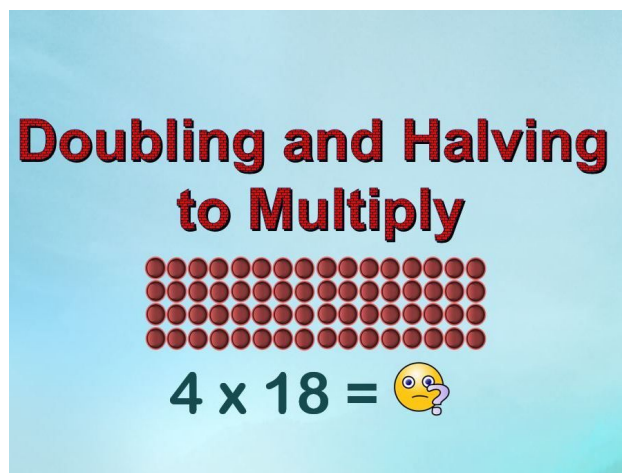
# Lesson from KDE to make connections

Problem Card Set A	Base Ten Card Set B	Area Model Card Set C	Distributive Property Card Set D	Partial Products Card Set E
Each pack of baseball cards has fifteen cards. How many cards are in twenty-two packs?			$(20 + 2) \times (10 + 5) =$ $20 \times 10 + 2 \times 10 + 20 \times 5 + 2 \times 5 =$	$\begin{array}{r} 15 \\ \times 22 \\ \hline 30 \\ 200 \\ \hline 220 \end{array}$
How many eggs are in twelve dozen?			$(10 + 2) \times (10 + 2) =$ $10 \times 10 + 2 \times 10 + 10 \times 2 + 2 \times 2 =$	$\begin{array}{r} 12 \\ \times 12 \\ \hline 24 \\ 120 \\ \hline 144 \end{array}$
The boy scouts traveled a distance of twenty-three feet in their boat. The girl scouts traveled eleven			$(20 + 3) \times (10 + 1) =$ $20 \times 10 + 3 \times 10 + 20 \times 1 + 3 \times 1 =$	$\begin{array}{r} 11 \\ \times 23 \\ \hline 33 \\ 220 \\ \hline 253 \end{array}$

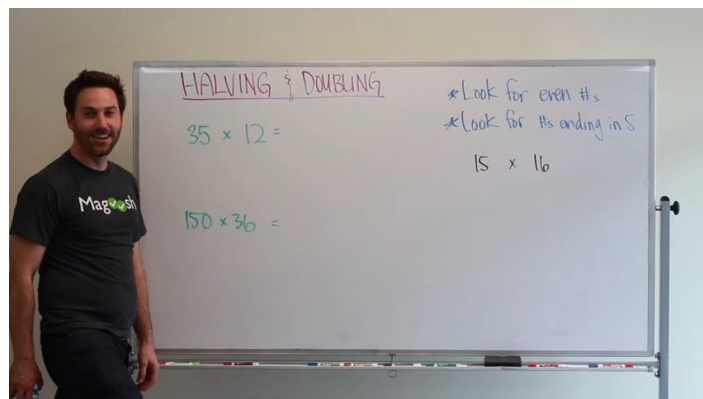
# Multi-Digit Multiplication Math Story Matching

- Start with Set A, B, C
- Match the story, area model and base ten card
- Students justify their thinking
- Then add Set D and E
- Students justify their thinking

# Halving and Doubling Strategy



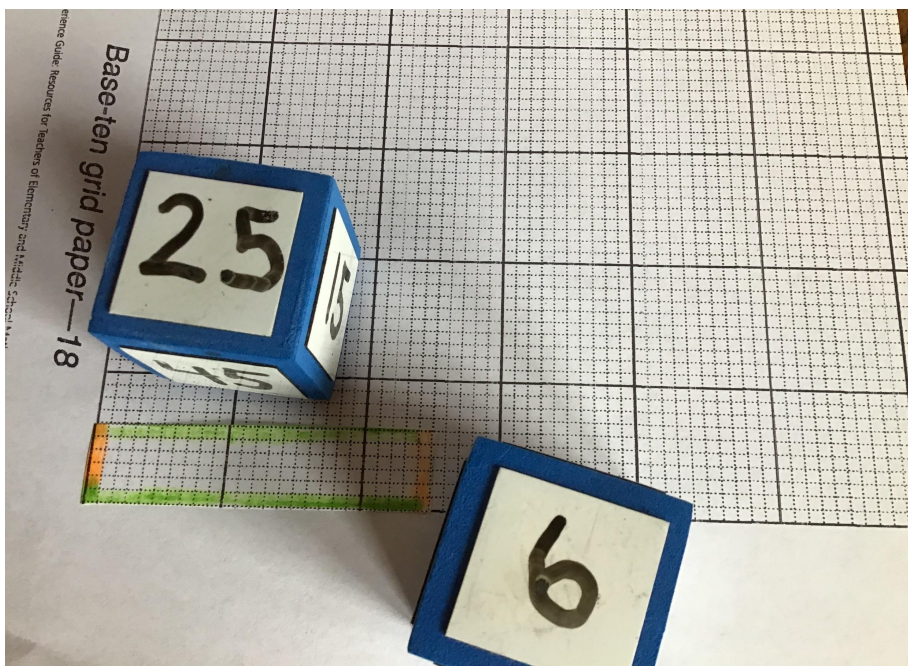
Click on images to play video





# Nice and Easy (halving and doubling)

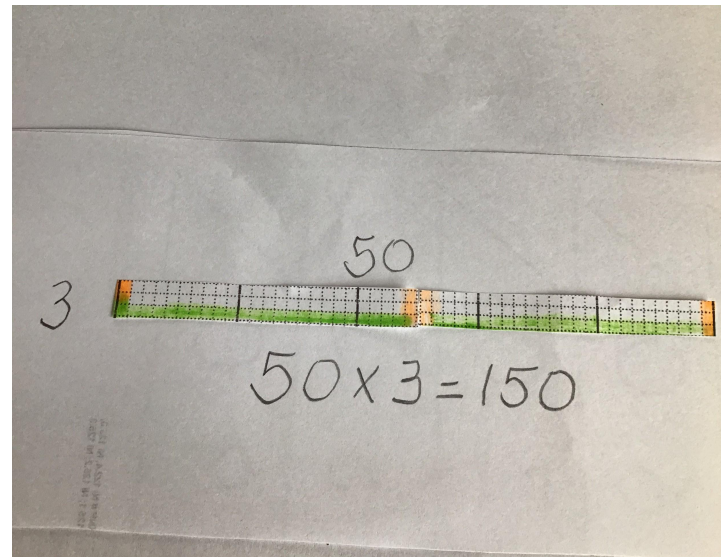
- Player 1 roll the cubes.
- Say aloud the multiplication sentence represented by the number cubes.
- Draw that area model on the base ten grid paper and cut out.





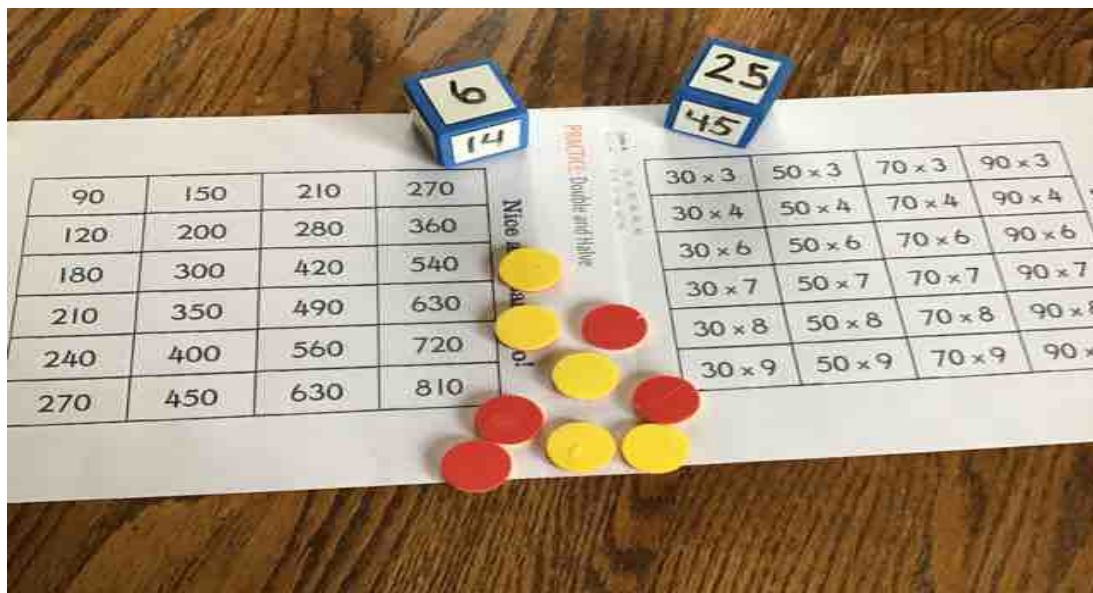
# Nice and Easy (halving and doubling)

- Cut the area model in half to create a new multiplication equation.
- Double one factor and half the other to figure out the equivalent multiplication sentence.

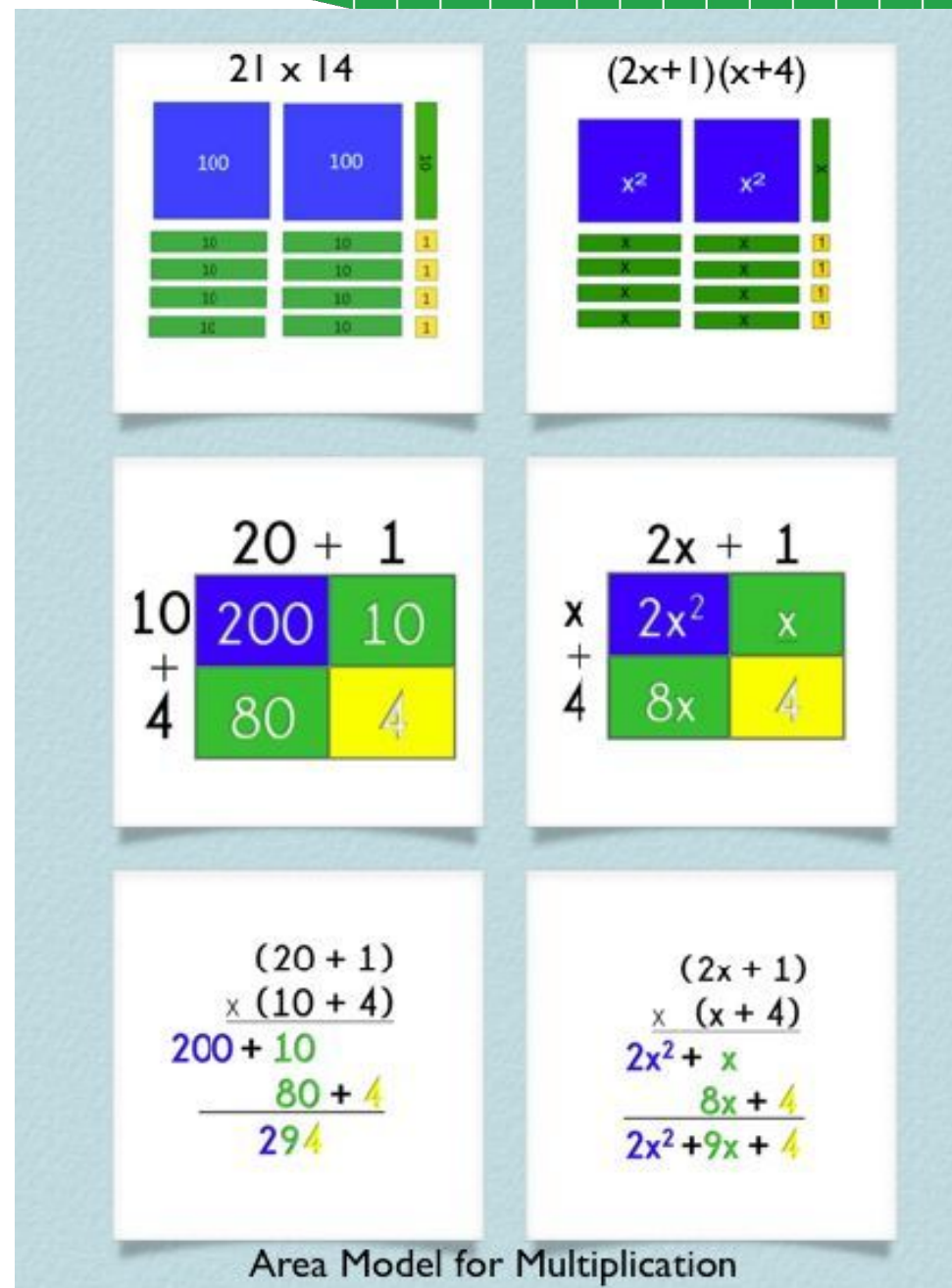


# Nice and Easy (halving and doubling)

- Place a counter on the matching multiplication sentence on the *Nice and Easy* game board.
- Calculate and say the product and place a counter on the corresponding product on the *Nice and Easy Too* game board.



Modeling is the  
key to  
conceptual  
understanding.



# Virtual Manipulatives

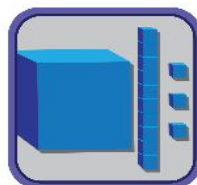
<https://www.didax.com/math/virtual-manipulatives.html>



120 Number Board



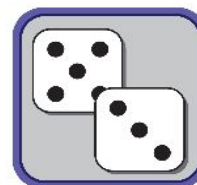
Color Tiles



Base Ten Blocks



Math Balance



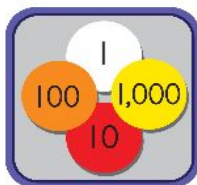
Dice



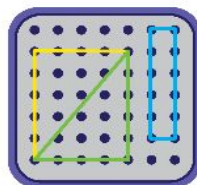
Spinners



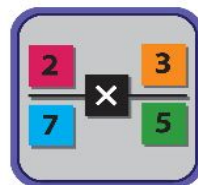
Pattern Blocks



Place Value Disks



Geoboard



Prime Factor Tiles



Algebra Tiles



# Toy Theater



MATH

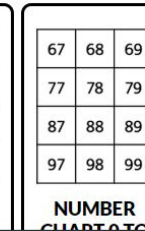
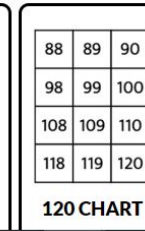
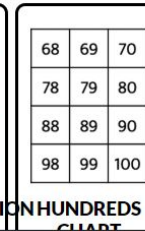
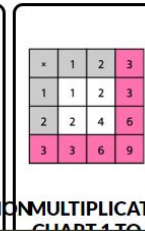
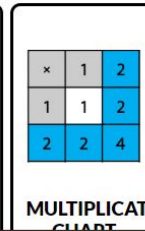
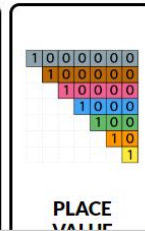
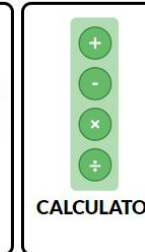
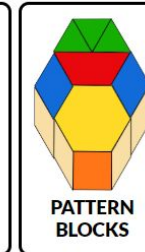
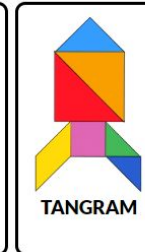
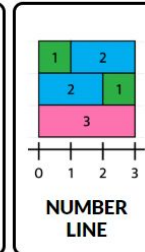
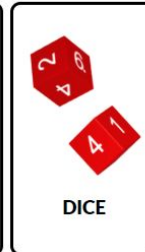
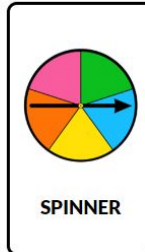
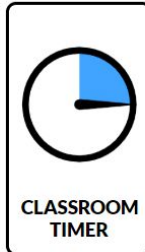
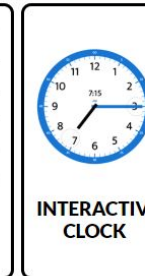
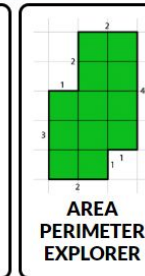
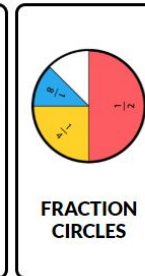
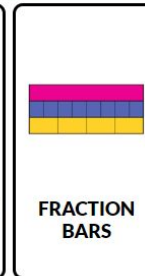
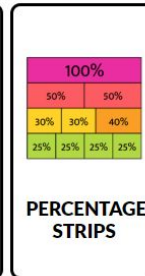
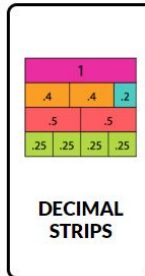
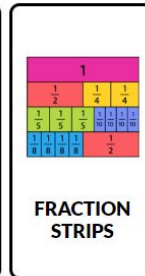
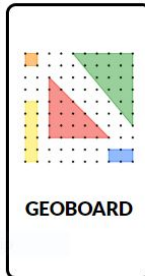
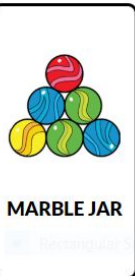
READ

ART

MUSIC

PUZZLE

GAME



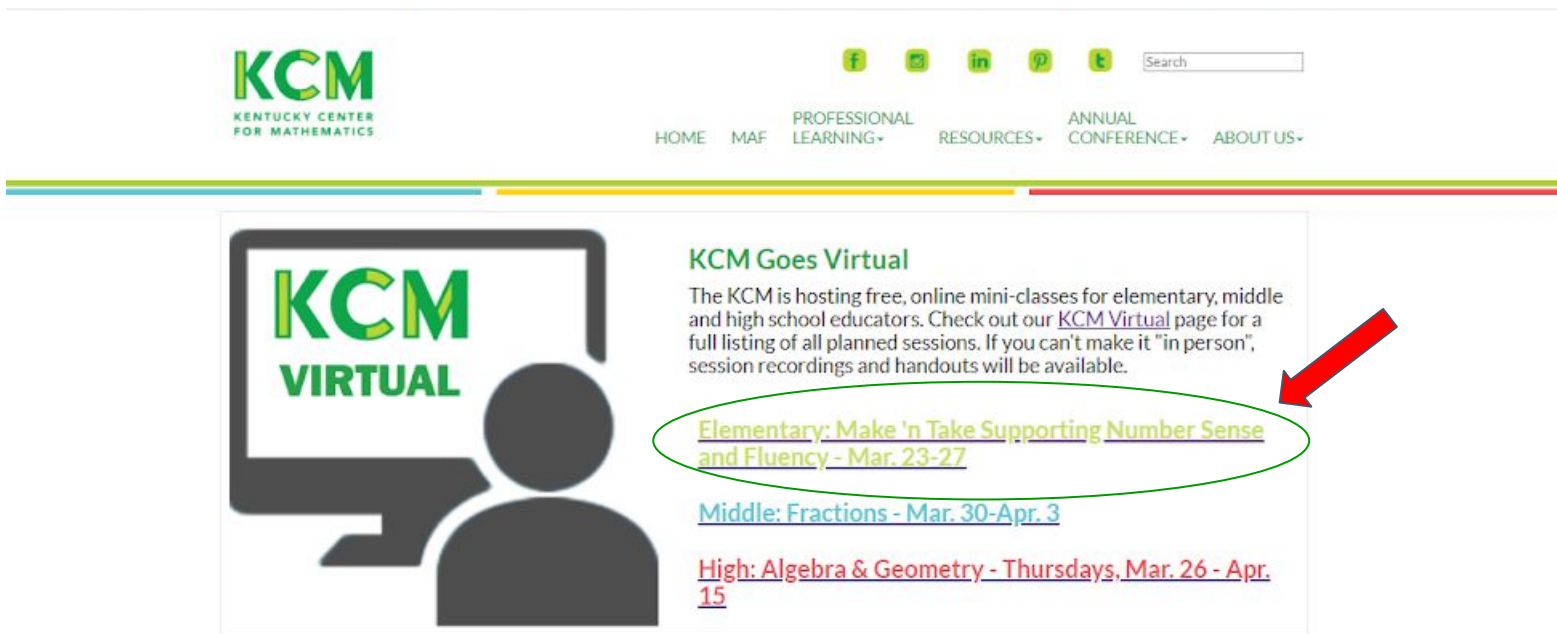
# Dreambox at home FREE for 90 days!

<https://www.dreambox.com/at-home>



# Visit Our Website

[www.kentuckymathematics.org](http://www.kentuckymathematics.org)



**KCM**  
KENTUCKY CENTER  
FOR MATHEMATICS

f t in y t Search

HOME MAF PROFESSIONAL LEARNING+ RESOURCES+ ANNUAL CONFERENCE+ ABOUT US+

---

**KCM**  
VIRTUAL

**KCM Goes Virtual**

The KCM is hosting free, online mini-classes for elementary, middle and high school educators. Check out our [KCM Virtual](#) page for a full listing of all planned sessions. If you can't make it "in person", session recordings and handouts will be available.

[Elementary: Make 'n Take Supporting Number Sense and Fluency - Mar. 23-27](#)

[Middle: Fractions - Mar. 30-Apr. 3](#)

[High: Algebra & Geometry - Thursdays, Mar. 26 - Apr. 15](#)

# Upcoming Virtual Professional Learning

MARCH 30 - APRIL 3  
2:00-2:30 PM EST

 **Let's Do Math!**

*with KCM Regional Consultants*

Monday, March 30 - Open Middle Fractions

Tuesday, March 31 - Shell Formative Assessment

Wednesday, April 1 - Connecting Representations

Thursday, April 2 - Open Middle Proportional Reasoning

Friday, April 3 - Multiplying Fractions



# We are here to support our teachers!

Your host:

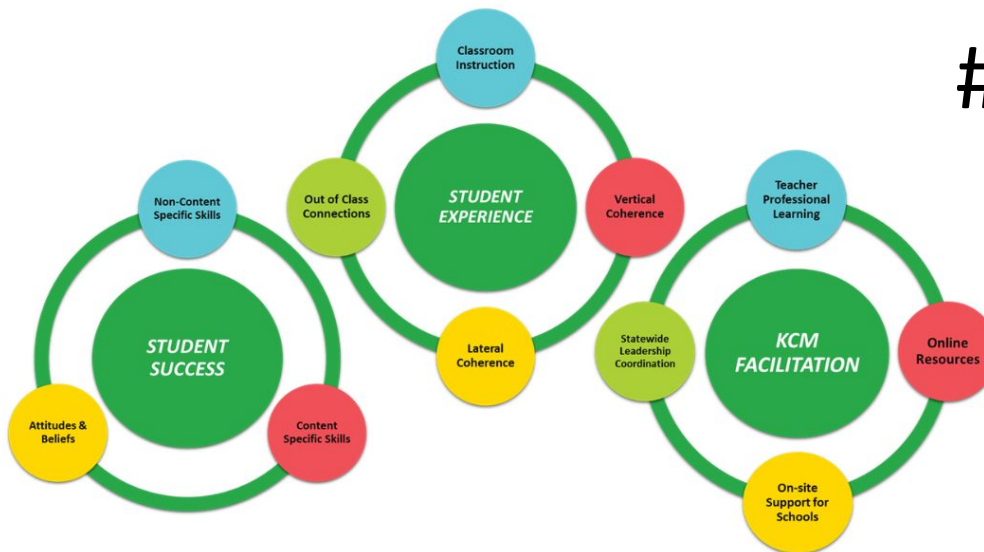
**Belle Rush**



Regional Consultant  
Kentucky Center for Mathematics  
[bsrush180@yahoo.com](mailto:bsrush180@yahoo.com)

# KCM Support for Educators

- Kentucky Center for Mathematics is here to support our KY educators
- We are aspire to be a national leader in mathematics education



#BetterTogether  
#TeamKCM